

Aufgabe 1

```
def f(n):
    if n == 2:
        return 1
    else:
        return 2*n + f(n-1)

print(f(6))
```

$$\begin{aligned}
 f(6) &= 2*6 + f(5) \\
 &= 2*6 + [2*5 + f(4)] \\
 &= 2*6 + [2*5 + [2*4 + f(3)]] \\
 &= 2*6 + [2*5 + [2*4 + [2*3 + f(2)]]] \text{ Base Case} \\
 &= 2*6 + [2*5 + [2*4 + [2*3 + 1]]] \\
 &= 2*6 + [2*5 + [2*4 + 7]] \\
 &= 2*6 + [2*5 + 15] \\
 &= 2*6 + 25 \\
 &= 37
 \end{aligned}$$

Aufgabe 2

```
def f(n):
    if n < 2:
        return 3
    else:
        return n + f(n-3)

print(f(11))
```

$$\begin{aligned}
 f(11) &= 11 + f(8) \\
 &= 11 + [8 + f(5)] \\
 &= 11 + [8 + [5 + f(2)]] \\
 &= 11 + [8 + [5 + [2 + f(-1)]]] \text{ Base Case} \\
 &= 11 + [8 + [5 + [2 + 3]]] \\
 &= 11 + [8 + [5 + 5]] \\
 &= 11 + [8 + 10] \\
 &= 11 + 18 \\
 &= 29
 \end{aligned}$$

Aufgabe 3

```
def f(n):
    if n == 6:
        return 2
    else:
        return 1 + f(n+1)

print(f(3))

f(3) = 1 + f(4)
      = 1 + [1 + f(5)]
      = 1 + [1 + [1 + f(6)]] Base Case
      = 1 + [1 + [1 + 2]]
      = 1 + [1 + 3]
      = 1 + 4
      = 5
```

Aufgabe 4

```
def f(n):
    if n < 2:
        return 2
    else:
        return 2*f(n-3)

print(f(10))

f(10) = 2 * f(7)
       = 2 * [2 * f(4)]
       = 2 * [2 * [2 * f(1)]] Base Case
       = 2 * [2 * [2 * 2]]
       = 2 * [2 * 4]
       = 2 * 8
       = 16
```

Aufgabe 5

```
def f(n):
    if n < 1:
        return 2
    else:
        return n*f(n-1)

print(f(4))

f(4) = 4 * f(3)
      = 4 * [3 * f(2)]
      = 4 * [3 * [2 * f(1)]]
      = 4 * [3 * [2 * [1 * f(0)]]] Base Case
      = 4 * [3 * [2 * [1 * 2]]]
      = 4 * [3 * [2 * 2]]
      = 4 * [3 * 4]
      = 4 * 12
      = 48
```

Aufgabe 6

```
def f(n):
    if n < 2:
        return n
    elif n % 2 == 0:
        return 3 + f(n-1)
    else:
        return 1 + f(n-2)

print(f(6))

f(6) = 3 + f(5)          # n=6 gerade
      = 3 + [1 + f(3)]    # n=5 ungerade
      = 3 + [1 + [1 + f(1)]] # n=3 ungerade/Base Case
      = 3 + [1 + [1 + 1]]
      = 3 + [1 + 2]
      = 3 + 3
      = 6
```